

⑦ Se  $f_1(n) = O(g_1(n))$  allora

$$\exists e_1, m_0' : f_1(n) \leq e_1 g_1(n) \quad \forall n > m_0'$$

Se  $f_2(n) = O(g_2(n))$  allora

$$\exists e_2, m_0'' : f_2(n) \leq e_2 g_2(n) \quad \forall n > m_0''$$

Se  $f_1(n) + f_2(n) = O(g_1(n) + g_2(n))$  allora

$$\exists e_3, m_0''' : f_1(n) + f_2(n) \leq e_3 (g_1(n) + g_2(n)) \quad \forall n > m_0'''$$

$$m_0''' = \max(m_0', m_0'')$$

$$e_3 = e_1 + e_2$$

DA RIVEDERE  
SULL'ALTRO  
QUADERNO

$$f_1(n) = \Omega(g_1(n))$$

$$f_2(n) = \Omega(g_2(n))$$

$$f_1(n) + f_2(n) \geq e_3 [g_1(n) + g_2(n)]$$

$$f_1(n) + f_2(n) \geq e_1 g_1(n) + e_2 g_2(n) - (e_2 - e_1) g_2(n)$$

$$f_1(n) + f_2(n) \geq e_1 g_1(n) + g_2(n) (e_2 - e_2 + e_1)$$

$$f_1(n) + f_2(n) \geq e_1 g_1(n) + g_2(n) e_1$$

$$f_1(n) + f_2(n) \geq e_1 (g_1(n) + g_2(n))$$

$$\Rightarrow e_3 = e_1$$