

$$\sum_{i=1}^k i = 1 + 2 + 3 + 4 + \dots + k$$

$$\sum_{i=1}^k i = 1 + 2 + 3 + 4 + \dots + (k-1) + k +$$

$$+ k + (k-1) + \dots + 2 + 1 =$$

$$(k+1) + (k+1) + \dots + (k+1) = \frac{k(k+1)}{2} = \sum_{i=1}^k i$$

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$$T(n) = \begin{cases} 1 & n \leq 1 \\ aT(n/c) + b n^d & \text{otherwise} \end{cases}$$

$$T(n) = \begin{cases} O(n^k) & \text{if } a < c^k \\ O(n^k \log n) & \text{if } a = c^k \\ O(n^{\log_c a}) & \text{if } a > c^k \end{cases}$$