

$A[0, \dots, m-1]$

DIVIDE ET IMPERIA

~~8/10/20~~

$SUM(A, j, k)$

IF $j == k$ return $A[j] \cdot \text{pow}(2, j)$;

$x \leftarrow (j+k)/2$

~~return~~ $A \leftarrow SUM(A, j, x)$;

~~return~~ $B \leftarrow SUM(A, x+1, k)$;

return $A+B$;

1 3 5 7 9

$$1 \cdot 2^0 + 3 \cdot 2^1 + 5 \cdot 2^2 + 7 \cdot 2^3 + 9 \cdot 2^4$$

j k
0, 4

x=2

$A(0,2)$

x=1

$A(0,1)$

x=0

$A(0,0)$

return $1 \cdot 2^0 \leftarrow A$

1, 1 $3 \cdot 2^1 \leftarrow B^+$

0 2

0 2

1

1

0 1

0

$SUM2(A, K, j, x)$

IF $j == x$ then return $A[j]$;

$L \leftarrow (j+x)/2$

$e \leftarrow SUM2(A, K, j, L)$;

$D \leftarrow SUM2(A, K, L, x)$;

return $(e+x) \bmod K$